

Nonlinear Optical Response of Organic–Inorganic Halide Perovskites

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Supporting Information

ABSTRACT: Metal halide perovskites have exhibited excellent properties as absorbers in solar cells, but this may simply be the first of many applications for this intriguing class of materials. Here, we report the nonlinear optical response of triio dide $(CH_3NH_3PbI_3)$ and mixed halide $(CH_3NH_3PbI_{3-x}Cl_x)$ perovskite absorbers. The results show that they have large nonlinear refractive index (NRI), 3 orders of magnitude larger than that of silicon. Particularly, the NRI of $CH_3NH_3PbI_{3-x}Cl_x$ is more than two times larger compared to that of $CH_3NH_3PbI_3$. Meanwhile, both of them have been proven to possess saturable absorption effects with small



nonlinear absorption coefficients which indicate that they can maintain excellent absorption under high-intensity irradiation and are favorable to modulators toward large-energy pulsed laser. Taking into consideration the saturable absorption effect, we demonstrated a pulsed laser with the perovskite as a pulse modulator. These results above indicate the potential for perovskites to be employed in nonlinear optoelectronic devices.

KEYWORDS: metal halide perovskites, nonlinear optical response, Kerr effects, saturable absorption, pulse modulator

S olar energy conversion is considered as one of the likely keys solutions to satisfy the growing global energy demand.¹⁻³ Recently, extremely rapid progress has been made in organic—inorganic halide perovkites solar cells with the energy conversion efficiencies already exceeding 20%,⁴⁻¹¹ and if they make commercial success, the discovery will be a revolutionary moment for the progress of photovoltaics. Nevertheless, despite the superb performances, perovskite solar cells suffer from some weak points which still require effort to overcome, i.e., instability against humidity and an anomalous hysteresis effect in the current voltage, most likely originating from drifting mobile ions and interfacial traps.¹²

In physics, the absorption of light in semiconductors such as the perovskites belongs to a light-matter interaction process in which the electrons in the interacted materials resonate with the electric field of the irradiating optical signal and induce polarization. In the simplest form, assuming the dielectric response in an isotropic material, the relation between a generated polarization P and an electric field $E(\omega)$ of the excitation optical signal with the circular frequency ω is expressed as¹³

$$P = \varepsilon_0(\chi^{(1)}E(\omega) + \chi^{(2)}E^2(\omega) + \chi^{(3)}E^3(\omega) + ...)$$
(1)

where ε_0 is the dielectric permittivity of the vacuum, $\chi^{(n)}$ is the *n*th-order susceptibility consisting of real and imaginary parts $\chi_r^{(n)}$ and $\chi_i^{(n)}$, respectively, and $\chi^{(n)}$ is several orders of magnitude larger than $\chi^{(n+1)}$. Therefore, under weak radiation

such as terrestrial sun light, the polarization is proportional to the excitation electric field and $\chi^{(1)}$ is responsible for the linear optics such as linear absorption, emission, refraction, etc. In contrast, under higher levels of irradiation from sources such as lasers, nonlinear optical properties can be observed. In the linear optics, the bright light-emitting,¹⁴ broadband photodetecting,¹⁵ and random lasing¹⁶ were reported concerning the organic—inorganic halide perovskites as gain materials, beside the intensive investigation on the solar cells.

Concerning the crystal structure, although there is some ambiguity over the precise space group due to imprecise determination of the position of the organic methylammonium (MA), MAPbI₃ perovskite is likely to be cento-symmetric^{17,18} indicating $\chi^{(2)} = 0$ at room temperature. Therefore, third-order nonlinear optics may be generated under irradiation by high-intensity light. Besides discovering the nature of a material, third-order nonlinear optics, including $\chi_r^{(3)}$ and $\chi_i^{(3)}$, have been extensively applied in optoelectronics.¹³ Thereby, considering the advantages such as low processing costs, the perovskites would play important roles in nonlinear optics and optical devices. In this scenario, there is no report concerning the nonlinear optical response of organic–inorganic halide perovskites, which might be associated with the anomalous hysteresis effect and guide the fabrication of optical devices. Here, we

Received: September 30, 2015 Published: January 25, 2016 show the third-order nonlinear optics of triiodide $(CH_3NH_3PbI_3)$ and mixed halide $(CH_3NH_3PbI_{3-x}Cl_x)$ perovskites absorbers under high-intensity irradiation including visible and near-infrared lasers. Afterward, we demonstrate a promising application as a saturable absorber for modulating the laser operation. This work is likely to stimulate significant effort toward realizing these and similar perovskites as nonlinear materials in optoelectronics.

RESULT AND DISCUSSION

Nonlinear Optical Response of Metal Halide Perovskites. We measured the absorption spectrum of $CH_3NH_3PbI_3$ and $CH_3NH_3PbI_{3-x}Cl_x$ thin film, as $1 - \log$ (transmission) with a V-570 JASCO UV/vis/NIR spectrophotometer and show the results in Figure 1. We observe absorption onset at around 800



Figure 1. Absorption spectra of triiodide $CH_3NH_3PbI_3$ and mixed halide $CH_3NH_3PbI_{3-x}Cl_x$ perovskites.

nm for both samples which is associated with the optical band gap of perovskite thin films. At longer wavelengths, their absorption as the function of wavelength toward near-infrared region gradually decreased. There should be no optical transition between the valence and conduction band in the region longer than 800 nm.^{18–20} Recently, the theoretical and experimental study about the organic—inorganic perovskites has discovered that there is a distribution of subgap trap states which are located under the conduction band,²¹ account for the largest fraction of electron-hole recombination, and would expand the absorption range. Therefore, the absorption at the wavelength longer than 800 nm should be generated by the transition terminated to the subgap trap states, and also manifests that both $CH_3NH_3PbI_3$ and $CH_3NH_3PbI_{3-x}Cl_x$ should have potentially optoelectronic applications in the wavelength range shorter than at least 2000 nm.

We employed the Z-scan technique to investigate the nonlinear optical response of $CH_3NH_3PbI_3$ and $CH_3NH_3PbI_{3-x}Cl_x$ layers with a PY61 mode-locked neodymium doped yttrium aluminum garnet (Nd:YAG) laser (pulse width of 40 ps and wavelength of 1.06 μ m) as the pump source. We show the configuration for Z-scan technique in Figure 2 and Supporting Information. The third-order nonlinear optics is contributed by the real part $\chi_r^{(3)}$ and the imaginary part $\chi_1^{(3)}$, which manifest as the NRI and nonlinear absorption as^{22,23}

$$a = n_0 + \gamma I$$

$$\alpha = \alpha_0 + \beta I$$
(2)

with

$$\chi_{\rm r}^{(3)} = 2n_0 \varepsilon_0 c \gamma$$

$$\chi_{\rm i}^{(3)} = \frac{n_0^2 \varepsilon_0 c^2}{\omega} \beta$$
(3)

where *n* and α are the refractive index and absorption coefficient, respectively, under the laser intensity of *I* within the sample, n_0 is the linear refractive index, γ is the NRI, β is the nonlinear absorption coefficient, ε_0 is the permittivity in vacuum, *c* is the speed of light in vacuum, and ω is the optical frequency. With the transmission at weak irradiation as a standard, we measured the nonlinear absorption and NRI using open-aperture and close-aperture techniques, respectively. The



Figure 2. Experimental setup for Z-scan technique. A neodymium doped yttrium aluminum garnet (Nd:YAG) laser with the center wavelength of 1064 nm and pulse width of 40 ps was used as the pump source. The output energy from the Nd:YAG laser was tuned with an optical attenuator. With a beam splitter, the Nd:YAG laser was split into two beams. One beam was used as the reference and another beam was focused by an objective lens. The perovskite solar cell sample perpendicularly oriented toward the incident beam and can be moved along the *z*-axis with a linear motorized stage. Two energy meters were employed to simultaneously detect the optical energy from different branches. An aperture was inserted in front of the detector energy meter and used for the investigation of nonlinear transmission. For the experiments at 532 nm laser, a type II cut potassium titanium oxygenic phosphate (KTP) single crystal was inserted after the Nd:YAG laser for the second harmonic generation and a dichroic mirror was placed after KTP crystal for transmitting 532 nm laser and reflecting 1064 nm laser.



Figure 3. Nonlinear absorption of $CH_3NH_3PbI_3$ and $CH_3NH_3PbI_{3-x}Cl_x$ samples under irradiation of a 1064 nm pulsed laser. (a) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$. (b) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$. (c) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$. (d) Experimental results and theoretical fitting for the nonlinear refractive index of $CH_3NH_3PbI_3$.

Table 1. Comparison between Organic-Inorganic Absorbers with Si, GaAs, and Silica

	532 nm		1.06 µm		
samples	nonlinear absorption coefficient (β : cm/MW)	saturable intensity $(I_{sat}: \text{ GW/cm}^2)$	nonlinear absorption coefficient (β : cm/MW)	saturable intensity $(I_{sat}: \text{GW/cm}^2)$	nonlinear refractive index $(\gamma: \times 10^{-15} \text{ m}^2/\text{W})$
CH ₃ NH ₃ PbI _{3-x} Cl _x	-203.3	0.5	-2.03	12.61	8.36
CH ₃ NH ₃ PbI ₃	-152	0.84	-2.25	12.71	3.74
CH ₃ NH ₃ PbBr ₃ (Single Crystal)	/	/	$8.2 \times 10^{-3} (at \ 0.8 \ \mu m)^{24}$	/	/
Si	/	/	/	/	$4.5 \times 10^{-3} (at \ 1.55 \ \mu m)^{13}$
Silica	/	/	/	/	$\sim 2 \times 10^{-5} (at \ 800 \ nm)^{28-30}$
GaAs	/	/	$-9.4 \times 10^7 (at 1.55 \ \mu m)^{24}$	7.9×10^{-8} (at 1.55 μ m) ²⁴	$3.25 \times 10^{-2} {}^{27}$

close aperture technique allows measuring the optical transmission change resulting from the combined consequence of the nonlinear absorption and nonlinear phase change induced by the NRI.

In the open aperture condition, we present the experimental results for the nonlinear transmission at the irradiation wavelength of 1064 nm in Figure 3, panels a and b for CH₃NH₃PbI₃ and CH₃NH₃PbI_{3-x}Cl_x, respectively. We find that the transmissions increase as the position of the samples approaches to the focused point z = 0, which indicates that both samples have saturable absorption properties. By theoretical fitting as shown in Supporting Information, we found that for CH₃NH₃PbI₃, the nonlinear absorption was β = -2.25 cm/MW with the saturable intensity $I_{sat} = 12.71$ GW/ cm², and for CH₃NH₃PbI_{3-r}Cl_r nonlinear absorption was β = -2.03 cm/MW with the saturable intensity $I_{sat} = 12.61$ GW/ cm², which is very similar to that of CH₃NH₃PbI₃. The saturable absorption intensity of the two samples is about 10⁸ times larger than that of gallium arsenide (GaAs) (79 W/ cm²),²⁴ which indicates that in the infrared wavelength range,

the absorption is difficult to be bleached, and the perovskites are supposed to have promising application in Q-switching as optical modulators for the generation of pulsed lasers with large pulses based on the theory of passively modulated pulsed lasers.²⁵ The saturable absorption can also be qualitatively understood based on the electronic band gap structure.²¹

When the samples are irradiated by weak light at 1064 nm, rather than be transferred from valence band to the conduction band, the photoexcited electrons would be trapped by the subgap trap states within the bandgap and will depopulate in the time scale of 100 μ s to 1 ms subsequently.²¹ However, under high intensity irradiation, the final electronic states will be fully occupied, blocking further absorption and transition from the valence to the subgap trap states, which induces the samples to exhibit saturable absorption in the time shorter than the recombination lifetime especially under the pump lasers with the pulse width of 40 ps.

Unlike the two-photon absorption in the near-infrared wavelength band of a single crystal $CH_3NH_3PbBr_3$ reported recently,²⁶ the saturable absorption of perovskites in our work



Figure 4. Nonlinear absorption of $CH_3NH_3PbI_3$ and $CH_3NH_3PbI_{3-x}Cl_x$ samples in open aperture condition under irradiation of a 532 nm pulsed laser. (a) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$. (b) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$. (b) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$. (b) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$. (b) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$. (b) Experimental results and theoretical fitting for the nonlinear absorption of $CH_3NH_3PbI_3$.

should be generated by the distribution of subgap trap states, and has the nonlinear absorption coefficient of 3 orders of magnitude larger than that of two absorption coefficient of CH₃NH₃PbBr₃ single crystal (8.2 cm/GW) as shown in Table 1. To rule out the possibility of contributions from PbI₂ from incomplete reaction or degradation of the perovskite film, we have measured the structures of the perovskite samples before and after the Z-scan and laser experiments by X-ray diffraction measurement. The results are shown in the Supporting Information, which shows that there was no PbI₂ from incomplete reaction or degradation of the perovskite film. We show the experimental results of the nonlinear transmission at the irradiation wavelength of 1064 nm in the close aperture condition in Figure 3, panels c and d for CH₃NH₃PbI₃ and $CH_3NH_3PbI_{3-x}Cl_x$ respectively. Via the theoretical fitting of the experimental results, the procedure for which we describe in Supporting Information, we obtain a NRI of $\gamma = 3.74 \times 10^{-15}$ m²/W for CH₃NH₃PbI₃, and $\gamma = 8.36 \times 10^{-15} \text{ m}^2/\text{W}$ for CH₃NH₃PbI_{3-x}Cl_x. The nonlinear refractive index of the perovskites is therefore, respectively, 10^3 and 10^2 times larger than those of Si ($\gamma = 4.5 \times 10^{-18} \text{ m}^2/\text{W}$)¹³ and GaAs ($\gamma = 3.25$ × 10^{-17} m²/W),²⁷ both of which have been identified as excellent absorbers in solar cells and exciting materials for nonlinear optoelectronics, and is 10⁵ times larger than that of silica $(\gamma = 2 \times 10^{-20} \text{ m}^2/\text{W})$,²⁸⁻³⁰ which has been extensively applied in the nonlinear waveguides in the advantages of sizes and easiness of preparation. On the basis of nonlinear optical theory, it can be derived that the distortion of electron clouds and the rotation of molecular dipoles formed by the CH₃⁺ and NH_2^- taking place in few picoseconds³¹⁻³³ are responsible for this nonlinear optical response of refractive index on the incident pump power. The difference of NRI indicates that the introduction of Cl⁻ ions, or the impact this has on the formed perovskite crystals, by some means, results in a slight structural destabilization leading to the redistribution of the delocalized electrons in CH₃NH₃PbI_{3-x}Cl_x, just like the difference of NRI between fullerene C₆₀ and its derivatives.³⁴ Compared with CH₃NH₃PbI₃, we can get that the contribution of distorted octahedral to the NRI is $\gamma = 4.62 \times 10^{-15} \text{ m}^2/\text{W}$ larger than that of CH₂NH₂PbI₂, which confirms that the conduction and valence band are predominately determined by the PbI₄X₂ (with X = Cl or I) octahedral in agreement with the theoretical calculation,¹⁶ and displays that electrons in CH₃NH₃PbI_{3-x}Cl_x films are much more weakly bound than those in CH₃NH₃PbI₃. Moreover, the large NRIs of the two perovskites indicate that their refractive indexes are sensitive to the intensity of light and should have promising applications in optoelectronics such as

optical modulation, frequency-shifting by four-wave mixing, or Raman effects^{13,35,36} as tens of times more sensitive devices.

In the sunlight spectra, the peak intensity is located at about 500 nm, where light absorption promotes band gap transition. The nonlinear absorption at this wavelength band is important for discovering the nature in a solar cell and might be helpful for understanding if there is an influence of the rotation of molecular dipoles forming the CH_3^+ and NH_2^- in possible ferroelectric domains upon the absorption coefficient in the perovskite solar cells. With the frequency doubling of the pump source by employing a potassium titanium oxygenic phosphate (KTP) single crystal, we realized a 532 nm pulsed laser for the investigation of nonlinear absorption. We show the results of nonlinear absorption of CH₃NH₃PbI₃ and CH₃NH₃PbI_{3-x}Cl_x in Figure 4a,b. Fitting the experimental results, we determine the nonlinear absorption coefficient with $\beta = -152$ cm/MW and saturable intensity of $I_{sat} = 0.84 \text{ GW/cm}^2$ for CH₃NH₃PbI₃ and $\beta = -203.3$ cm/MW and $I_{sat} = 0.5$ GW/cm² for CH₃NH₃PbI_{3-x}Cl_x. In the present studied time scales, the laser generates the electrons that transfer from valence band to conduction band and the local field may also induce an orientation of the molecular dipoles. The influence of the two effects above on the absorption of the perovskites is shown as the nonlinear absorption coefficient. Under irradiation by simulated sunlight (AM 1.5), the generated carrier intensity can be calculated with the rate equation:³

$$N_{\text{carrier}} = \frac{\alpha I \tau}{h\omega} \tag{4}$$

where τ is the carrier recombination time and *h* is the Planks constant. On the basis of eqs 2 and 4, the carrier densities with and without nonlinear absorption show almost no change with the values of 0.26×10^{15} cm³ for CH₃NH₃PbI₃ and 7.3×10^{15} cm^3 for CH₃NH₃PbI_{3-x}Cl_x which shows that the carrier density of $CH_3NH_3PbI_{3-x}Cl_x$ is about 30 times larger than that of CH₃NH₃PbI₃ under same irradiation due to the difference in the carrier recombination lifetime.⁴ To obtain a 10% change in absorption, reduction of absorption coefficients, due to the nonlinear effects, we would need to increase the solar intensity to be about 132 and 222 MW/cm² for CH₃NH₃PbI₃ and CH₃NH₃PbI_{3-x}Cl_x, respectively. The results also denote that the orientation of molecular dipoles in the perovskites has almost no influence on the absorption and photon generated carrier concentrations when they are applied as absorbers in solar cells, which are in agreement with the recent reported result in perovskites solar cells.³⁸ Therefore, the influence of carrier intensity induced by the orientating of the molecular



Figure 5. Pulsed laser performance with $CH_3NH_3PbI_3$ as the optical modulator at 1.06 μ m. (a) Average output power with the increase of incident pump power with the threshold of 5.2 W. (b) Repetition rate with the increase of incident pump power in the range from 99 to 237 kHz. (c) Pulse train with the repetition rate of 99 kHz and pulse width of 660 ns. (d) Modulated pulsed Nd:YGG laser spectra.

dipoles on the hysteresis effect could be ruled out, consistent with the hysteresis in the solar cells primarily originating from macroscopic polarization due to the presence of mobile ionic species.³⁴

Passively Q-Switched Laser. On the basis of the measurement of nonlinear response, here we demonstrate the application as a pulsed modulator in solid-state lasers at 1.06 μ m. We show the output power and repetition rate with the incident pump power in Figure 5a,b. We observe that the output power and repetition rate increase with the pump power giving the maximum output power of 29 mW in the range of 99-237 kHz and the temporal pulse width decreases from 660 to 305 ns. These results are typical for passive Q-switching. We show the typical pulse train with a repetition rate of 99 kHz under the pump power of 5.6 W in Figure 5c. On the basis of the average output power repetition rate, we calculate the pulse energy with a maximum value of about 131 nJ with the laser wavelength located at 1.06 μ m as shown in Figure 5d. These results have been obtained in a simple spin-coated thin film on a glass substrate. It is likely that the result can be substantially improved by further optimization in the modulation depth of the perovskites, the doping concentration or tuning of the composition of the crystal and designing of a laser cavity.

CONCLUSIONS

We have investigated the nonlinear optical response of the organic—inorganic perovskites absorbers $CH_3NH_3PbI_3$ and $CH_3NH_3PbI_{3-x}Cl_x$ including the NRI and nonlinear optical absorption coefficient induced by the real and imaginary parts of third-order nonlinear dielectric permittivity, respectively. Our detailed comparisons among organic—inorganic perovskites with Si, silica, and GaAs, which are presented in Table 1, show that the perovskites have large NRI and saturable absorption properties, suggesting it has promising applications in the generation of pulsed lasers. The breaking of PbI_4X_2 (with X = Cl or I) octahedral symmetry with introduction of Cl anions could be responsible for the larger NRI of $CH_3NH_3PbI_{3-x}Cl_x$ compared with that of $CH_3NH_3PbI_3$ and indicates the strong tenability of perovskite semiconductors by

subtle variations in composition. On the basis of the nonlinear optical response, we demonstrated a pulsed IR laser with the perovskites as an optical modulator. All of these results identify the perovskites as also having promising applications in other optoelectronics in addition to the extensively studied solar cells and the presented optical modulator.

EXPERIMENTAL METHODS

Material Preparation. In the present study, a set of commercial far-ultraviolet quartz glass wafers ($\Phi 25 \times 1 \text{ mm}^3$) were employed as the substrates, which were polished and uncoated. Both the CH₃NH₃PbI₃ and CH₃NH₃PbI_{3-x}Cl_x thin films were deposited on the substrates by a solution-processed method in Supporting Information. In particular, the CH₃NH₃PbI₃ thin film was obtained by a sequential deposition method, and the CH₃NH₃PbI_{3-x}Cl_x thin film was prepared by simply mixing the PbCl₂ and CH₃NH₃I precursor solution with a ratio of 1:3. The thickness of perovskite thin films was controlled to be around 400 nm. Top-down scanning electron microscope (SEM) images of as-prepared perovskite thin films were characterized by a field emission scanning electron microscopy (JEOL JSM-7500F) (Figure S1).

Laser Design. A fiber-coupled diode laser was employed as the pump source with the emission of 808 nm. A neodymium doped yttrium gallium garnet Nd: $Y_3Ga_5O_{12}$ (Nd:YGG) single crystal was used as the gain material cut along the <111> direction with the dimensions of 3 mm × 3 mm × 6 mm. The neodymium doping concentration was 1 at%. The detailed description for the laser configuration is shown in the Supporting Information. The CH₃NH₃PbI₃ was inserted into the two-mirror resonator near the concave output coupler in case the pump light influenced the optical switching performance.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsphoto-nics.5b00563.

The detailed preparation processes of perovskites absorbers $CH_3NH_3PbI_3$ and $CH_3NH_3PbI_{3-x}Cl_x$ thin film, the experimental setup for Z-scan technique, and the detailed description for the laser configuration with perovskite as optical modulator; structures of the perovskite thin films before and after the Z-scan and laser experiments. (PDF)

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Notes

The authors declare no competing financial interest.

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